

# Efficient acceleration of relativistic magneto-hydrodynamic jets: theoretical study

*(Toma & Takahara 2013, Prog. Theor. Exp. Phys., 2013, 3E02)*

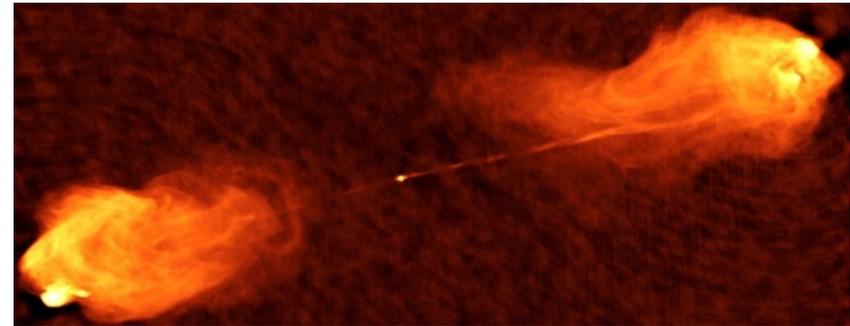
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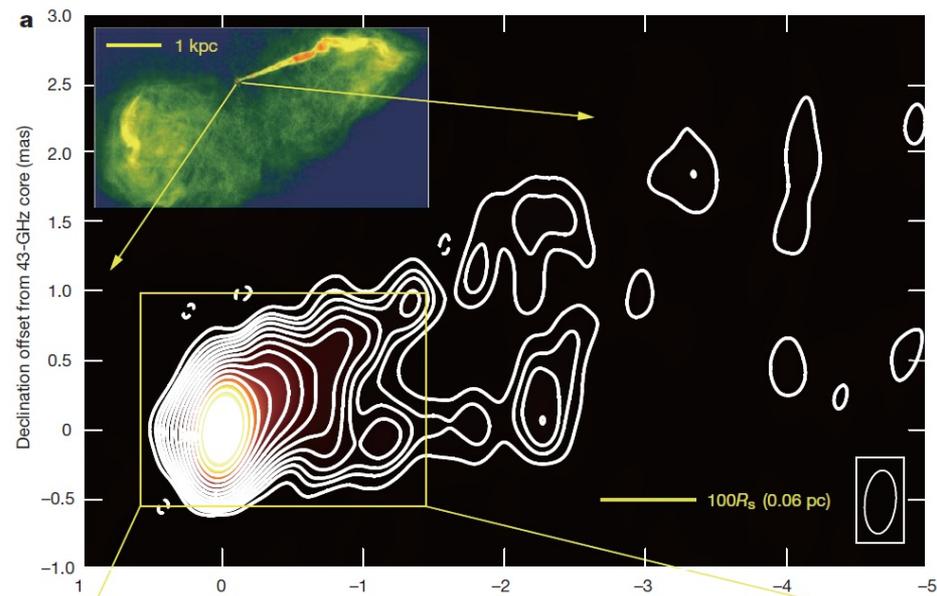
Collaboration with F. TAKAHARA

# Relativistic Jets

- Active galactic nuclei, gamma-ray bursts, etc.
- Lorentz factor  $\Gamma \sim 10-10^3$ (?)
- One of the major problems in astrophysics
- Those objects are candidates of high-energy CR,  $\nu$ , and GW emitters.

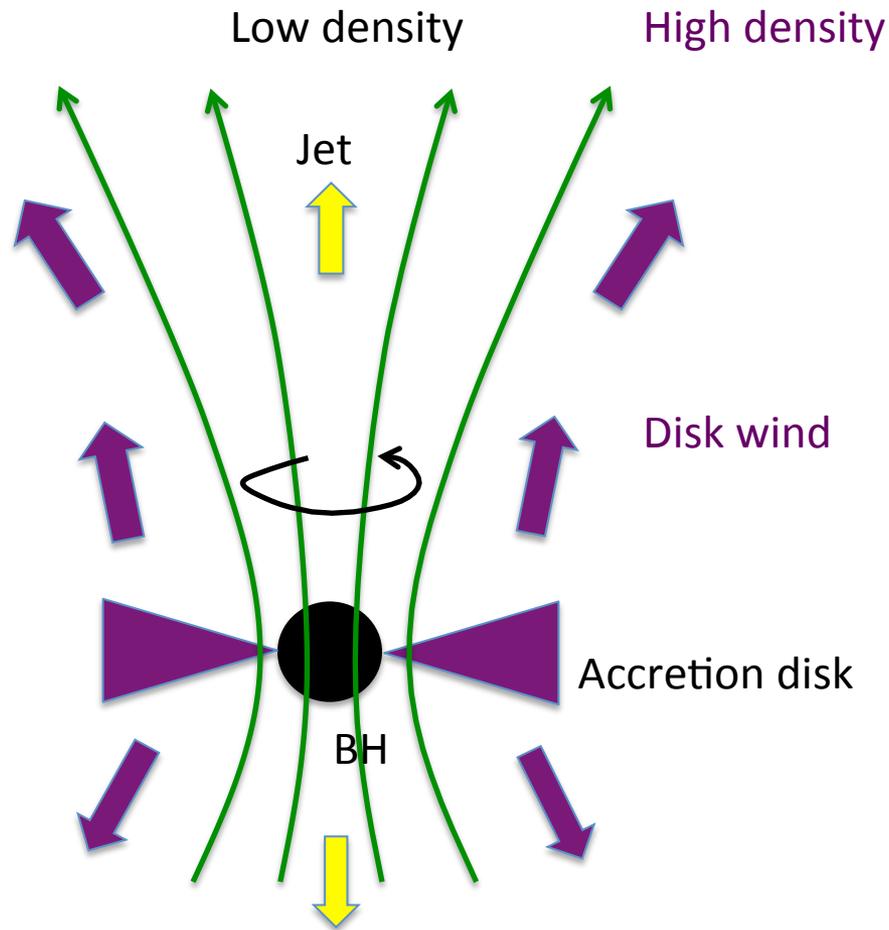


Radio image of Cygnus A



M87 (Hada+ 2011)

# Promising Scenario

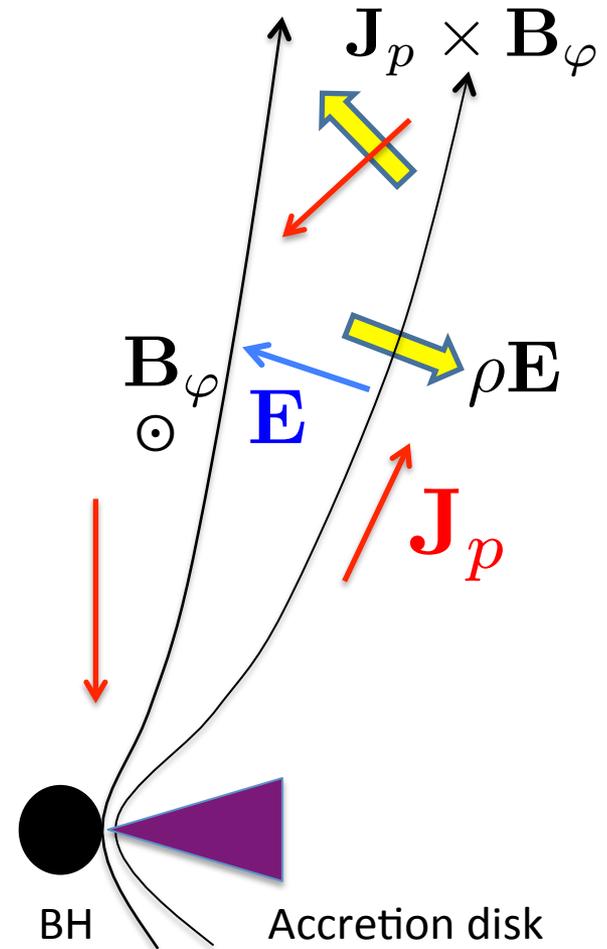


(see numerical simulations by J. McKinney, A. Tchekhovskoy, etc.)

- **Steady extraction of rotational energy of accretion disk or BH** (Goldreich & Julian 1969; Blandford & Znajek 1977; see also KT & Takahara 2014) → **Poynting-dom jet** (Kino+ 15)
- Mass loading mechanism unknown. Unsteady process or diffusion of high-energy hadrons? (KT & Takahara 2012; Kimura et al. 2015)
- **Matter acceleration by Lorentz force**
- **Collimation by external pressure**

# Matter acceleration, collimation

- Particles are accelerated by  $J \times B$  force (= energy flux conversion from Poynting to kinetic)
- $J \times B$  force also collimates the flow
- But  $\rho E$  force expands the flow
- **In the relativistic flow,  $E \sim -v_p \times B_\phi \sim B_\phi$  beyond the light cylinder  $\rightarrow B_\phi^2$  stress is not effective for collimation (except for the region near the axis)** (Komissarov+09; Lyubarsky 09)
- **Efficient acceleration requires expansion of magnetic flux tube ( $\sim$  de Laval nozzle)** (e.g. Begelman+94; KT & Takahara 2013)

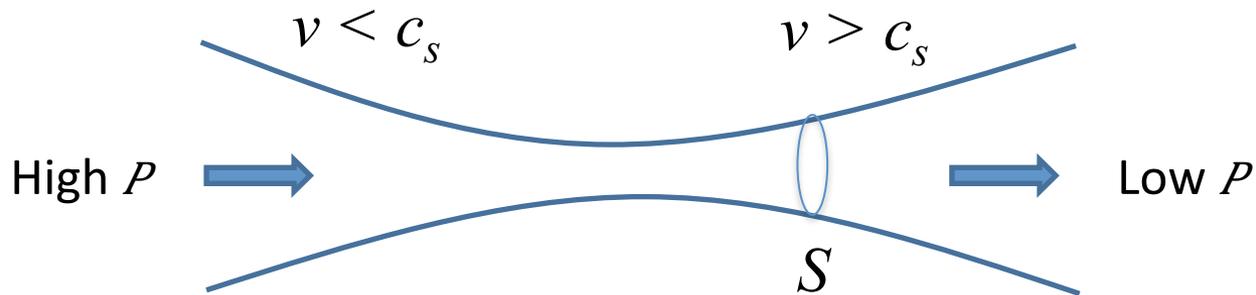


# Acceleration mechanism

De Laval nozzle:

one-dimensional hydrodynamic case

$$\left(1 - \frac{v^2}{c_s^2}\right) \frac{dv}{v} = \frac{-dS}{S}$$



Two-dimensional magneto-hydrodynamic case

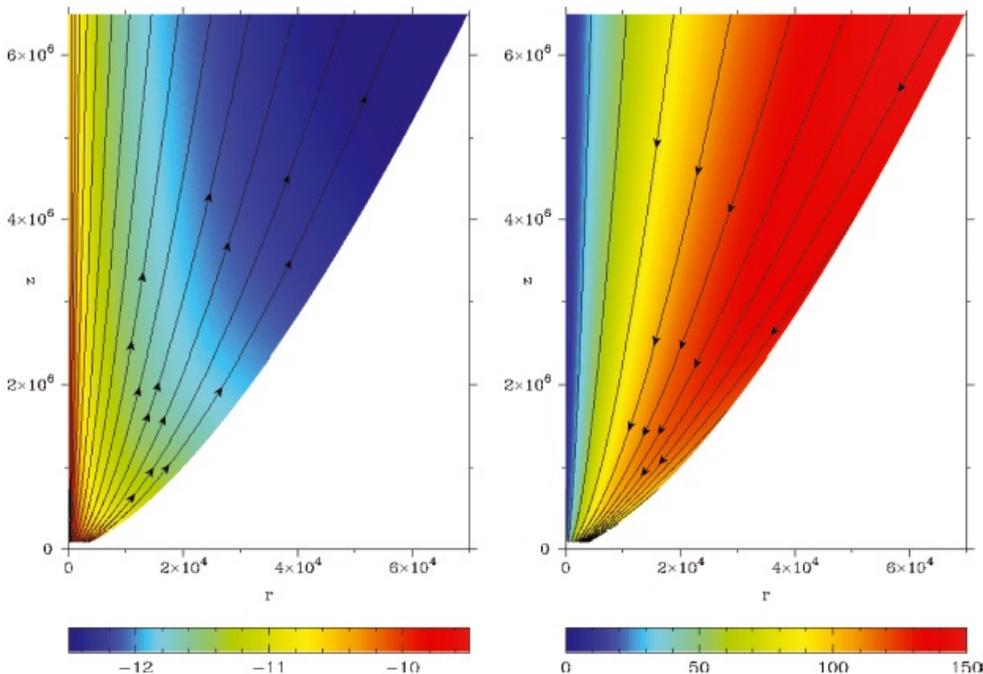
$$S = B_p r^2$$

$$\left(1 - \frac{u_f^2}{u_p^2}\right) \frac{d\Gamma}{\mathcal{E} - \Gamma} + \frac{c^2 \Gamma_{\text{in}}}{r^2 \Omega^2 \Gamma} \frac{d\Gamma}{u_p} + \left(1 + \frac{2\Gamma_{\text{in}}}{\Gamma}\right) \frac{(-v_\phi dv_\phi)}{v_p^2} = \frac{-dS}{S}.$$

Magnetic flux tube must be expanded when the super-fast flow is accelerated.

# Acceleration mechanism

(Komissarov, Vlahakis, Konigl & Barkov 2009)



Poloidal B field lines  
& Density

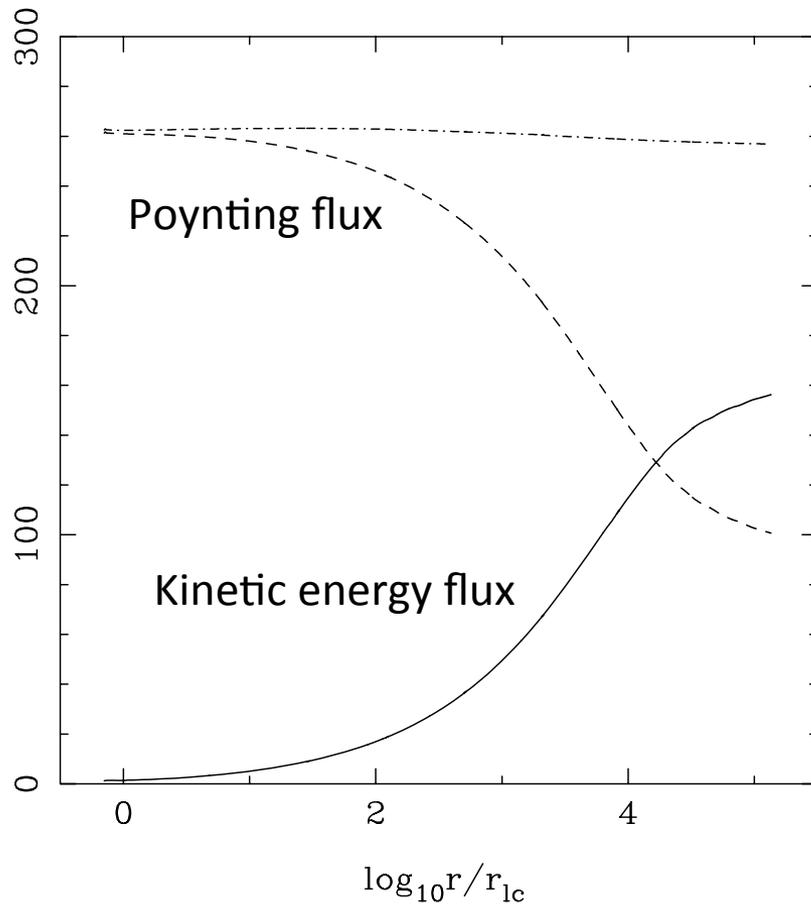
Poloidal currents  
& Lorentz factor

- Steady axisymmetric MHD solution
- BH gravity neglected
- External rigid wall (parabolic)
- Gradual acceleration
- Collimation near the axis leads to expansion of outer region

(see also Lyubarsky 2009;  
Asada, Nakamura et al. 2014)

# Acceleration efficiency

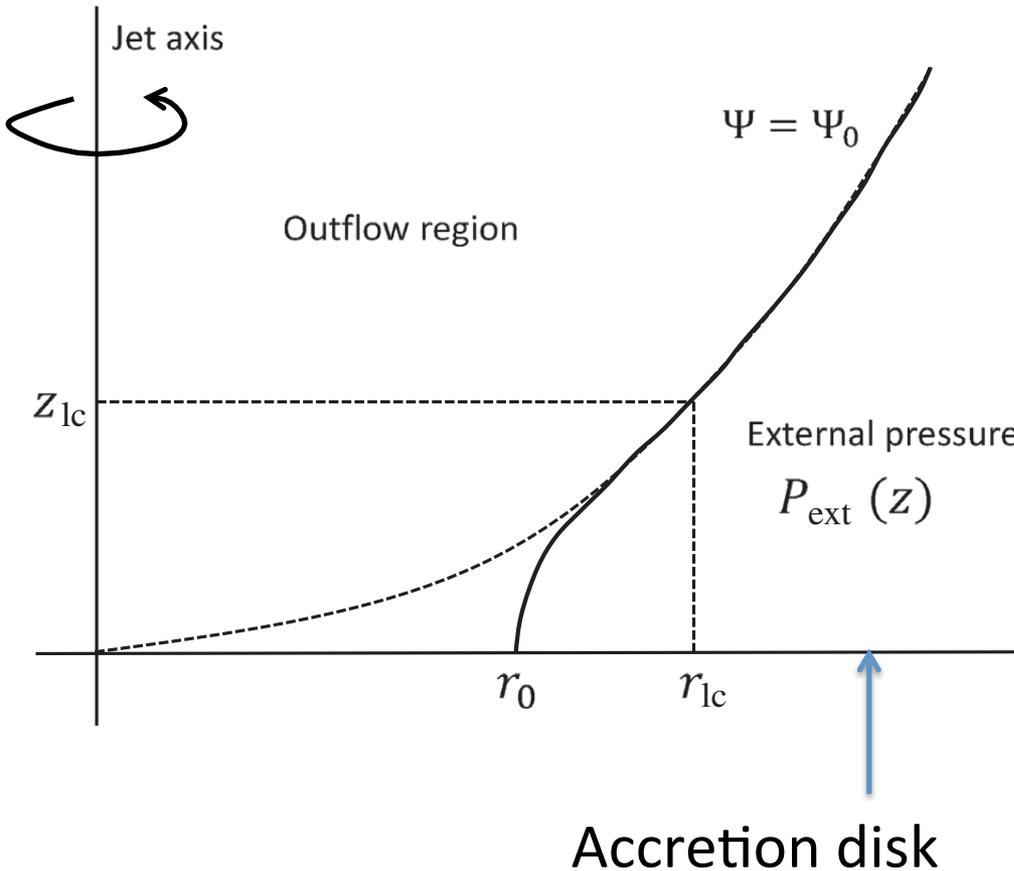
(Komissarov, Vlahakis, Konigl & Barkov 2009)



- Poynting/kinetic  $\sim 1$  at  $r \sim 10^4 r_{lc}$  ( $z \sim 10^6 r_{lc}$ ) which is extremely large distance
- **But observations of blazars imply Poynting/kinetic  $< 0.1$  at  $r \sim 10^3 r_{lc}$**  (e.g. Kino+ 2002; Sikora + 2005)
- (Efficient magnetic dissipation?)

We look for boundary conditions for more efficient acceleration

# Field line near the boundary

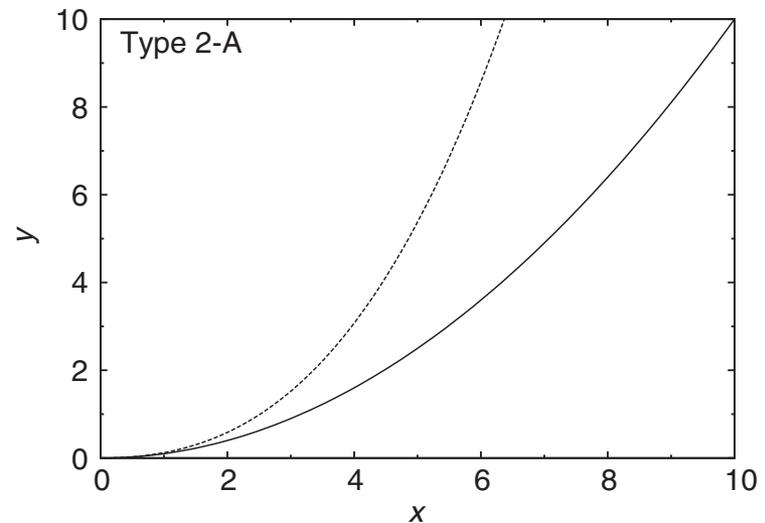
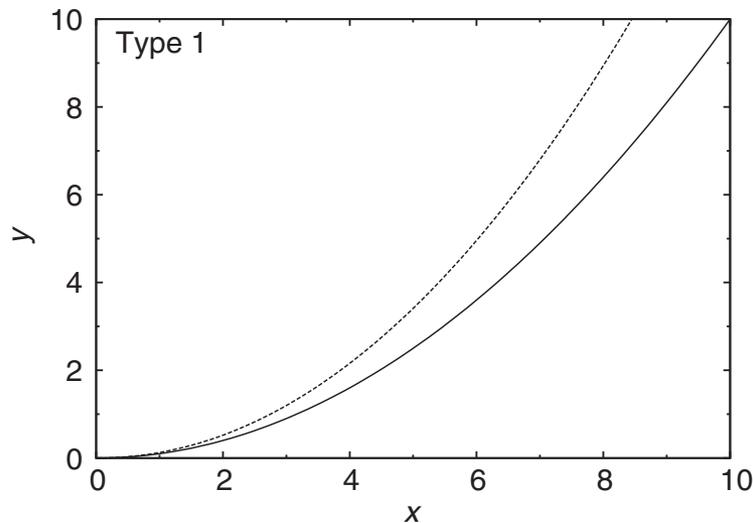


- Focus on the fluid motion along the field line near the boundary (not solving transverse structure)
- Assume the shape of the boundary
- Look for field structure for efficient acceleration
- External pressure

$$\left( \frac{B_p^2 + B_\phi^2 - E^2}{8\pi} \right) \Big|_{\Psi=\Psi_0} = P_{\text{ext}}(z).$$

# Examples of field line structure

- Boundary:  $y = 0.1 x^2$
- Plot the field line of  $\Psi = 0.95 \Psi_0$

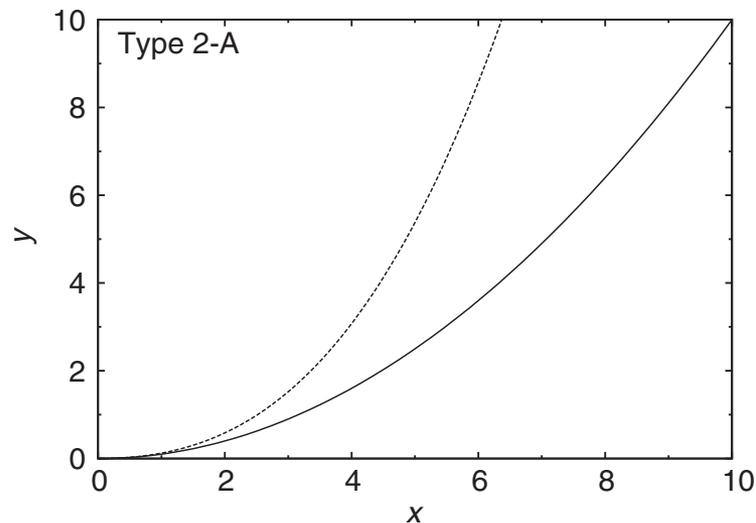
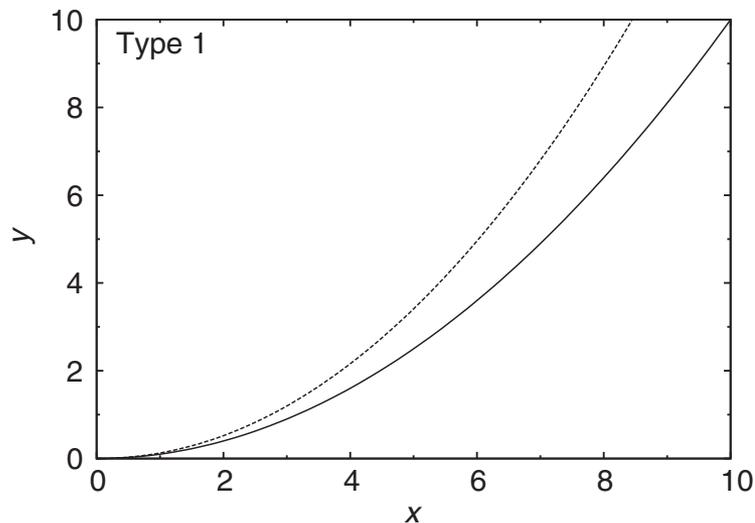


$$y = D \left( \frac{x}{d} \right)^{a(\psi)},$$

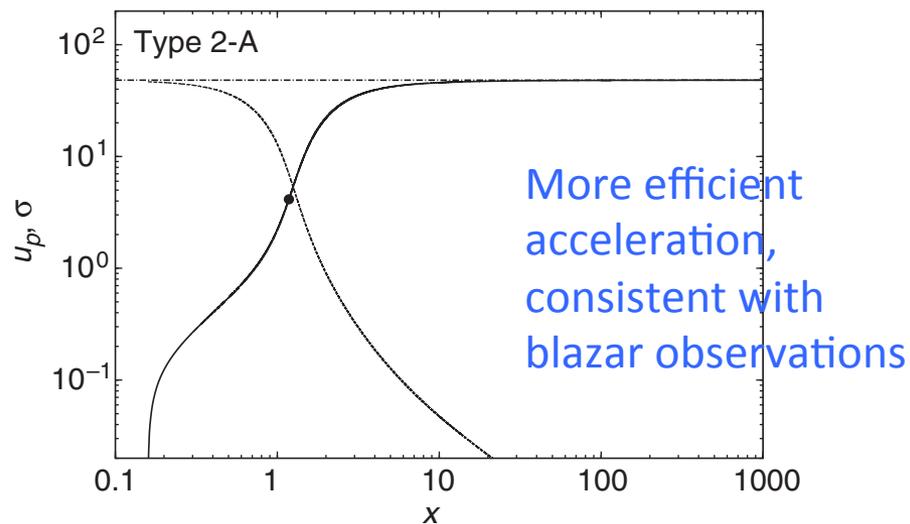
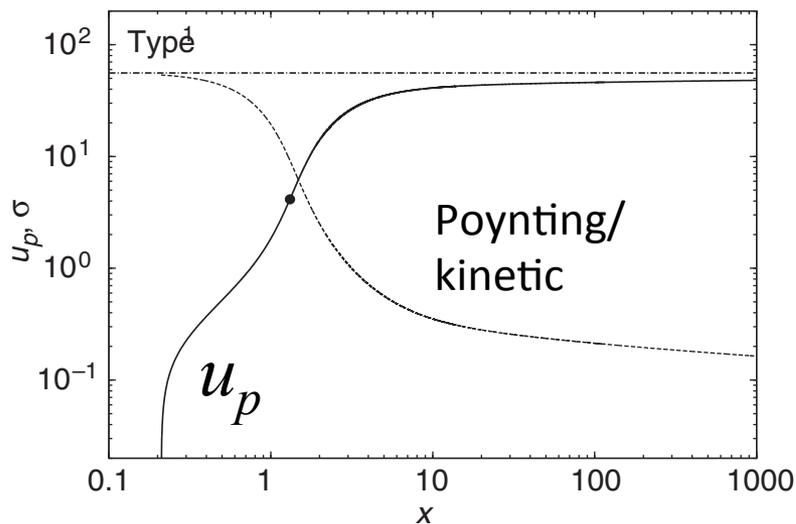
$$y = A_0 x^{a_0} + F(\psi) x^b,$$

More efficient acceleration

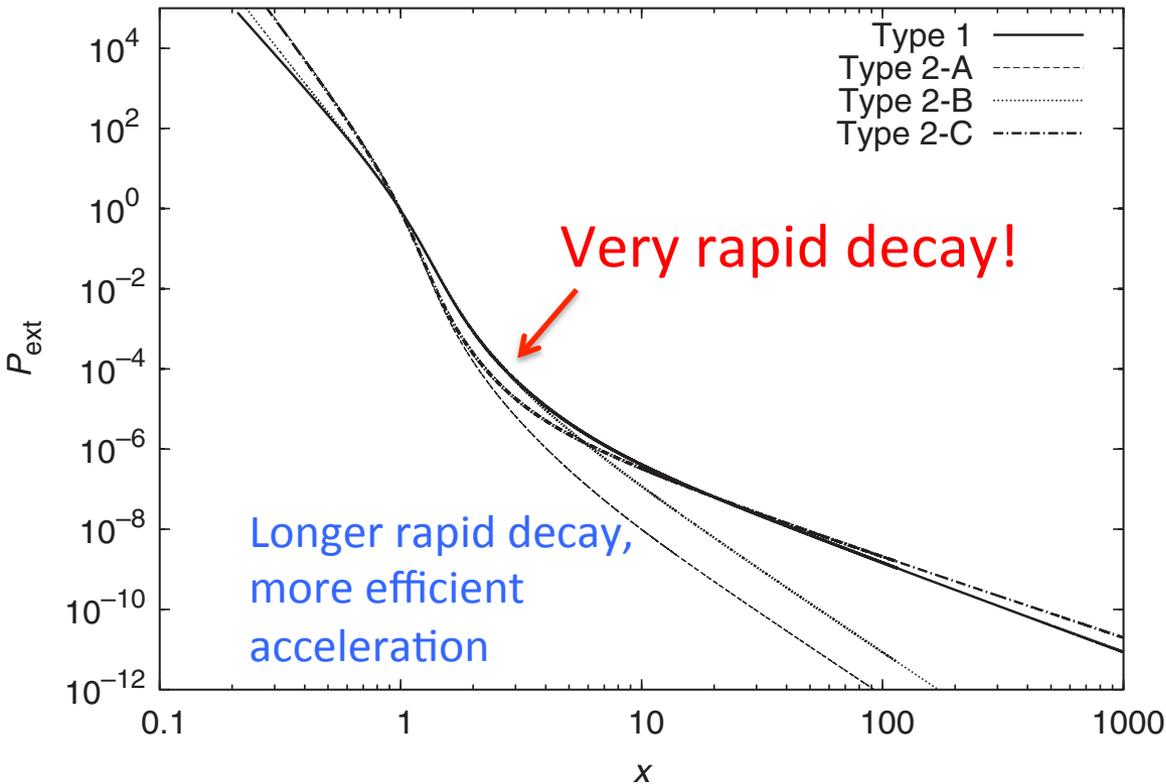
# Solutions of cold MHD wind eq.



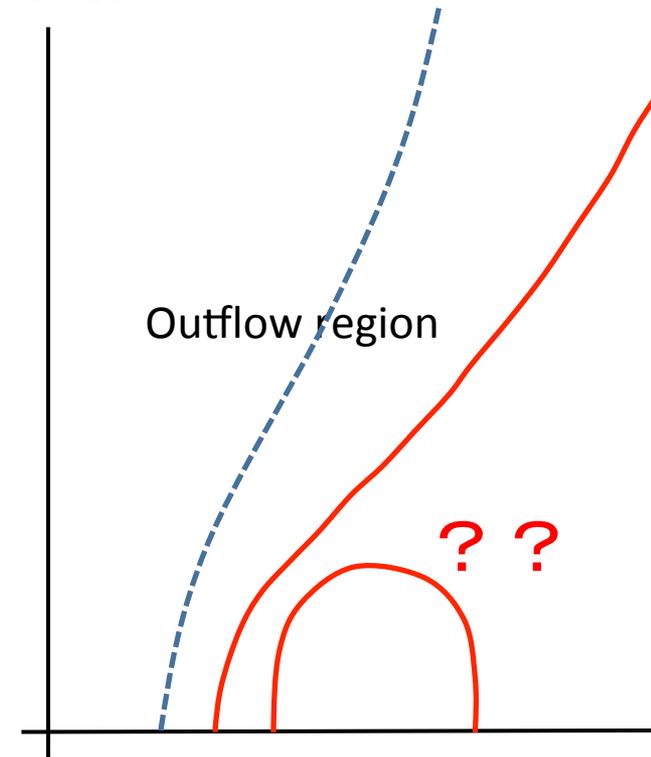
Both cases show Poynting/kinetic  $\sim 0.3$  at  $r \sim 3 r_{lc}$



# Solutions: external pressure



Jet axis



External medium could be the corona with closed field loops?

# Summary

- MHD jet can accelerate the particles to relativistic speeds (e.g. Komissarov+ 2009) (consistent with radio observations of M87 jet... Asada+ 2014; Kino+ 2015)
- More efficient acceleration is needed for explaining the blazar gamma-ray spectra
- We show boundary conditions for very efficient acceleration, which correspond to very rapid decay of external pressure
- Another possibility is efficient magnetic dissipation (whose mechanism is not clear yet)